

Planning Guide

Advanced Additive to Advanced Multiplicative

Addition and Subtraction

E CA AC EA **AA** AM AP

| Strategy | Numeracy book reference | Unit in this book | Page |
|--|---|---|--|
| Choose critically from a range of strategies to solve addition and subtraction problems. | <i>Teaching Addition, Subtraction and Place Value (Book 5)</i> No specific reference but this unit revises all Advanced Additive addition and subtraction strategies. | 1 - Addition and subtraction revision <i>We are learning to use an efficient way to solve addition and subtraction problems.</i> | 18 to 21 |
| Use multiplication to solve addition and subtraction problems where common factors can be found. | <i>Teaching Addition, Subtraction and Place Value (Book 5)</i> Multiple Ways to Add and Subtract Average Ability | 2 - Using multiplication to solve addition and subtraction problems <i>We are learning to use multiplication and common factors to solve addition and subtraction problems.</i> <i>We are learning to add and subtract by averaging numbers.</i> | 22 to 23 24 |
| | <i>Teaching Number Sense and Algebraic Thinking (Book 8)</i> Adding Sequences | <i>We are learning to use multiplication to add and subtract a series of whole numbers, fractions and decimals – except questions 4 to 6.</i> <i>We are learning to use multiplication to add and subtract a series of whole numbers, fractions and decimals – questions 4 to 6.</i> | 25 to 27 26 |
| | | | |
| Solve addition and subtraction problems with integers (positive and negative numbers). | <i>Teaching Addition, Subtraction and Place Value (Book 5)</i> Dollars and Bills Hills and Dales <i>Teaching Number Sense and Algebraic Thinking (Book 8)</i> 6 Minus 8 Does Work | 3 - Adding and subtracting integers <i>We are learning to add integers.</i> <i>We are learning to add and subtract integers in the real world.</i> <i>We are learning to add and subtract integers.</i> <i>We are learning a method of subtracting using negative numbers.</i> | 28 to 29 30 to 33 34 to 38 39 |

Multiplication and Division

| Strategy | Numeracy book reference | Unit in this book | Page |
|---|--|---|----------|
| Use standard place value to solve multiplication problems (distributive property). | <i>Teaching Multiplication and Division (Book 6)</i> Multiplication Smorgasbord | 4 - Multiplying using place value <i>We are learning to multiply using place value.</i> | 40 to 43 |
| Use tidy numbers (rounding and compensating) to solve multiplication problems (distributive property). | <i>Teaching Multiplication and Division (Book 6)</i> Multiplication Smorgasbord | 5 - Multiplying using rounding and compensating <i>We are learning to multiply using rounding and compensating.</i> | 44 to 47 |
| Use place value and tidy numbers (rounding and compensating) to solve division problems. | <i>Teaching Multiplication and Division (Book 6)</i> Paper Power <i>Note: The written forms part of this lesson is addressed by unit 20.</i> | 6 - Dividing using two different strategies <i>We are learning to divide using place value or rounding and compensating.</i> | 48 to 51 |
| Use proportional adjustment like doubling and halving, thirding and trebling, to solve multiplication problems. | <i>Teaching Multiplication and Division (Book 6)</i> Cut and Paste | 7 - Multiplying using proportional adjustment <i>We are learning to multiply using doubling and halving.</i> | 52 to 55 |
| Use proportional adjustment to solve division problems. | <i>Teaching Multiplication and Division (Book 6)</i> Proportional Packets | 8 - Dividing using proportional adjustment <i>We are learning to solve division problems using how many times one number will go into another.</i> | 56 to 59 |
| Simplify division problems by changing both numbers (halving, thirding etc). | <i>Teaching Multiplication and Division (Book 6)</i> The Royal Cooking Lessons | 9 - Dividing by changing both numbers <i>We are learning to solve division problems by changing them to simpler problems that have the same answer.</i> | 60 to 63 |

| Strategy | Numeracy book reference | Unit in this book | Page |
|---|--|--|----------|
| Use proportional adjustment like doubling and halving, thirding and trebling, to solve multiplication and division problems. | <i>Teaching Number Sense and Algebraic Thinking (Book 8)</i> Doubling and Halving | 10 - Multiplying and dividing using proportional adjustment <i>We are extending applications of doubling and halving, trebling and thirding.</i> | 64 to 65 |
| | Multiply by 25 | 11 - Multiplying by 25 <i>We are learning a quick way to multiply by 25.</i> | 66 to 67 |
| Solve division and multiplication problems using reversibility. | <i>Teaching Number Sense and Algebraic Thinking (Book 8)</i> Reversals with Multiplication and Division | 12 - Exploring multiplication and division <i>We are learning how to reverse multiplication and division problems to make them easier.</i> | 68 to 70 |
| Know that changing the order in division matters. | To Turn or Not to Turn | <i>We are learning that changing the order in division matters.</i> | 71 |
| Use the equals sign appropriately. | The Equals Sign Again | <i>We are learning that the answer on the left of the equals sign is the same as the answer on the right of the equals sign.</i> | 72 to 73 |
| Solve multiplication and division problems that include zero. | Using 0 | <i>We are learning about multiplying and dividing by zero.</i> | 73 |
| Solve division problems that involve remainders, expressing the remainders as whole numbers, fractions or decimals, depending on the context. | <i>Teaching Multiplication and Division (Book 6)</i> Remainders | 13 - Dividing with remainders <i>We are learning to solve division problems that have remainders.</i> | 74 to 77 |

| Strategy | Numeracy book reference | Unit in this book | Page |
|--|---|--|------------------|
| Solve multiplication problems using an efficient strategy, knowing why that is the best strategy to use. | <i>Teaching Multiplication and Division (Book 6)</i> Multiplication Smorgasbord Cut and Paste | 14 - Multiplying by choosing a strategy <i>We are learning to multiply by choosing an efficient strategy.</i> <i>Note: This unit concentrates on students choosing an efficient strategy to use to solve multiplication problems and includes</i> <i>Using place value</i> <i>Using rounding and compensating</i> <i>Using proportional adjustment</i> <i>Other strategies.</i> | 78 to 85 |
| Solve division problems using an efficient strategy, knowing why that is the best strategy to use. | <i>Teaching Multiplication and Division (Book 6)</i> The Royal Cooking Lessons Proportional Packets Remainders | 15 - Dividing by choosing a strategy <i>We are learning to divide by choosing an efficient strategy.</i> <i>Note: This unit concentrates on students choosing an efficient strategy to use to solve division problems and includes</i> <i>Using place value</i> <i>Using rounding and compensating</i> <i>Using proportional adjustment</i> <i>Other strategies.</i> | 86 to 95 |
| Check the answer to multiplication problems by estimation. | <i>Teaching Number Sense and Algebraic Thinking (Book 8)</i> Checking Multiplication by Estimation | 16 - Estimating 1 <i>We are learning to check the answers to multiplication problems by estimation.</i> <i>Note: At the end of Estimating 2 there are more activities for practising estimation.</i> | 96 to 97 and 101 |
| Check the answer to division problems by estimation. | <i>Teaching Number Sense and Algebraic Thinking (Book 8)</i> Checking Division by Estimation | 17 - Estimating 2 <i>We are learning to check the answers to division problems by estimation.</i> | 98 to 101 |
| Use cross products to solve multi-digit multiplication problems. | <i>Teaching Multiplication and Division (Book 6)</i> Cross Products | 18 - Multiplying larger numbers <i>We are learning to multiply multi-digit whole numbers.</i> | 102 to 105 |

| Strategy | Numeracy book reference | Unit in this book | Page |
|---|---|--|------------|
| Use place value to solve multiplication and division problems, including written multiplication algorithms. | <i>Teaching Multiplication and Division (Book 6)</i> Paper Power | 19 - Multiplying using place value and written forms <i>We are learning to work out multiplication problems using written working forms.</i> | 106 to 109 |
| Use standard place value to solve division problems, including written forms. | <i>Teaching Multiplication and Division (Book 6)</i> Paper Power | 20 - Dividing using place value and written forms <i>We are learning to work out division problems using written working forms.</i> | 110 to 113 |
| Find the remainder of a division problem using the calculator. | <i>Teaching Number Sense and Algebraic Thinking (Book 8)</i> Finding remainders | 21 - Remainders on the calculator <i>We are learning to find remainders using the calculator.</i> | 114 to 115 |
| Use divisibility rules for 2, 3, 4, 5, 6, 8, 9. | <i>Teaching Multiplication and Division (Book 6)</i> Nines and threes | 22 - Dividing by nine and three <i>We are learning to decide if a number is divisible by nine and three.</i> | 116 to 119 |
| | <i>Teaching Number Sense and Algebraic Thinking (Book 8)</i> Divisibility Rules | 23 - Divisibility tests <i>We are learning some divisibility tests.</i> | 120 to 121 |
| Solve problems using a combination of all four operations including using the order of operations. | <i>Teaching Number Sense and Algebraic Thinking (Book 8)</i> Order of Operations | 24 - Order of operations <i>We are learning to calculate using the conventional order of operations.</i> | 122 to 125 |
| Use a range of mental and written strategies to solve multi-step problems that involve a combination of addition, subtraction, multiplication, and division with whole numbers. | <i>No specific Numeracy book reference</i> | 25 - Solving problems using all four operations <i>We are learning to solve problems using all four operations.</i> | 126 to 135 |

Algebraic Thinking

| Strategy | Numeracy book reference | Unit in this book | Page |
|--|---|--|---|
| Find out whether a number is prime or non-prime, and use primes to find the factors of a number. | <i>Teaching Number Sense and Algebraic Thinking (Book 8)</i> Prime Numbers Factor Trees The Seive of Eratosthenes | 26 - Prime numbers <i>We are learning to find prime numbers.</i> <i>We are learning to use factor trees to find all the prime factors of a number.</i> <i>This is included in “We are learning to find prime numbers” in the Prime Investigations section, question 3.</i> | 136 to 139 140 to 141 139 |
| Explore leap years and lunar years. | <i>Teaching Number Sense and Algebraic Thinking (Book 8)</i> Leap Years Turn of the Century The Lunar Year | 27 - All about years <i>We are learning to find which years are leap years and about the lunar year.</i> <i>Note: This unit consists of two investigations.</i> | 142 to 143 |
| Find the relationship between square numbers and square roots and geometric squares and the relationship between cube numbers, cube roots and geometric cubes. | <i>Teaching Number Sense and Algebraic Thinking (Book 8)</i> Squaring Square Roots Locating Square Roots Cubes and Cube Roots | 28 - Squares, square roots, cubes and cube roots <i>We are learning that squaring a number gives the area of a square that has sides of that length.</i> <i>We are learning that if we know the area of a square we can find the length of the side by finding the square root.</i> <i>We are learning how finding cubes and cube roots relates to finding volumes and sides of cubes.</i> | 144 to 145 146 to 147 148 to 149 |

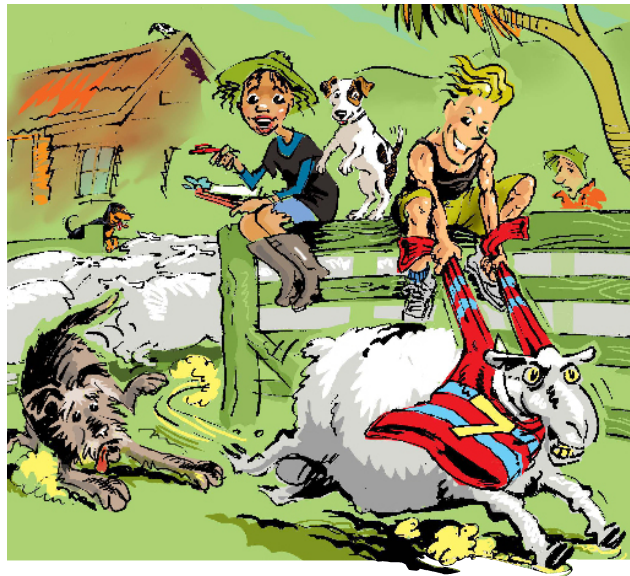
Number Knowledge

| Being developed | Numeracy book reference | Number knowledge in this book | Page |
|--|--|--|------|
| Identifies multi-digit numbers up to millions and the relationship between the place of a digit and its value. | <i>Teaching Number Knowledge (Book 4)</i> Number Fans Place Value Houses Number Hangman Reading Decimal Fractions More Reading Decimal Fractions | Number knowledge unit A <i>Place value</i> | 150 |
| Knows the number that is ten, hundred or a thousand times bigger or smaller than a given number. | <i>Teaching Number Knowledge (Book 4)</i> Digits on the Move | Number knowledge unit B <i>Multiplying and dividing by 10, 100 and 1000</i> | 151 |
| Recall the number of groupings of tens, hundred, and thousands that can be made from a number of up to seven digits. | <i>Teaching Number Knowledge (Book 4)</i> Arrow Cards Number Hangman Close to 100 Nudge Tens in Hundreds and More Estimating Zap | Number knowledge unit C <i>Thousands, hundreds, tens, ones and tenths</i> | 152 |
| Round whole numbers and decimals, with up to two places, to the nearest thousand, hundred, ten, whole number or tenth. | <i>Teaching Number Knowledge (Book 4)</i> Swedish Rounding Sensible Rounding | Number knowledge unit D <i>Rounding</i> | 155 |
| Order decimals to three places. | <i>Teaching Number Knowledge (Book 4)</i> Card Ordering Arrow Cards Rocket – Where Will It Fit? Squeeze – Guess My Number Bead Strings Who Wins? | Number knowledge unit E <i>Ordering numbers</i> <i>Note: There is more ordering of decimals in the Advanced Multiplicative Book 2 Number Knowledge section.</i> | 159 |

| Being developed | Numeracy book reference | Number knowledge in this book | Page |
|--|--|--|------------|
| Say the forwards and backwards decimal word sequences by thousandths, hundredths, tenths, ones, tens, etc, starting at any whole number. | <i>Teaching Number Knowledge (Book 4)</i> Number Fans Place Value Houses Number Hangman Skip-counting on the Number Line Hundreds Boards and Thousands Book Beep Lucky Dip | Number knowledge unit F <i>Counting on and back</i> | 161 |
| Say the number one-thousandth, one-hundredth, one-tenth, one, and ten, etc, before and after any given whole number. | <i>Teaching Number Knowledge (Book 4)</i> Number fans Skip-counting on the Number Line Lucky Dip | Number knowledge unit F <i>Counting on and back</i> | 161 |
| Recall the groupings of numbers to 10 that are in numbers to 100 and finds the resulting remainders, e.g. sixes in 38. | <i>Teaching Number Knowledge (Book 4)</i> Dividing – Think About Multiplying First | Number knowledge unit G <i>Dividing a two-digit number by a one-digit numbers</i> | 164 |
| Recognise and work with negative numbers in context. | <i>No specific number knowledge activities</i> | Number knowledge unit H <i>Negative numbers</i> | 165 |
| Recall multiplication and division facts to 10 x 10, and the corresponding division facts. | <i>Teaching Number Knowledge (Book 4)</i> Dividing – Think About Multiplying First Multiplication Flash Cards Loopy Multiplication Madness In And Out Bowl a Fact Beep Number Mats and Number Fans Bridges Addition Flash Cards | Number knowledge unit I <i>Number practice</i> <i>Note: There is only a little multiplication and division basic facts practice, as there is plenty of material available elsewhere.</i> <i>e.g Figure it out.</i> | 166 |

| Being developed | Numeracy book reference | Number knowledge in this book | Page |
|---|--|--|------|
| Identify factors of numbers to 100 including prime numbers. | <i>No specific number knowledge activities</i> | Number knowledge unit J <i>Factors</i> | 168 |
| Find common multiples of numbers to 10. | Beep | Number knowledge unit K <i>Multiples</i> | 170 |
| Convert between fractions and decimals such as tenths, fifths, thirds, halves and quarters. | Number Fans | Number knowledge unit L <i>Fractions and decimals</i> | 172 |
| Know the square numbers to 100 and the corresponding square roots. | <i>No specific number knowledge activities</i> | Number knowledge unit M <i>Squares and square roots</i> | 174 |
| Record the results of calculations using equations and diagrams. | <i>No specific number knowledge activities</i> | <i>Note: There is plenty of practice on this in all of the strategy units.</i> | |
| Carry out a short written algorithm for multiplication and division of a three-digit whole number by a single-digit number. | <i>No specific number knowledge activities</i> | <i>Note: There is plenty of practice on this in strategy units 19 and 20.</i> | |





New Zealand Curriculum Mathematics
Stage 7 Advanced Multiplicative Book 1
Addition, Subtraction, Multiplication, Division and Algebra